

he	Data	а			
rid	gender	age	education	address	salary
1001	М	24	High school	LA,CA	100K
1002	F	25	College	LA,CA	60K
1003	М	36	College	NY,NY	65K
1004	м	61	Graduate school	NY,NY	120K
1005	F	18	College	NY,NY	40K
1006	F	29	Graduate school	NY,NY	50K
1007	F	55	High school	SD,CA	35K
1008	м	45	Middle school	SD,CA	30K



#### Observations about Data Cubes ...

- How did a few tuples turn into so much data?
  - Many cells contain no data (or 0) • E.g. (M,60+,College,LA)
  - Many aggregation values are the same
  - E.g.(M, 20-30, HS, LA), (M, 20-30, LA), and (M,LA)

#### ... Observations about Data Cubes

#### Observations

- Curse of Dimensionality
- Sparsity
- Closed coverage
- Solutions
  - Partial computation of data cube
    - Iceberg Cube Shell Cube

#### Cell

- $a_i$  is either a value or \*
- A cell is a m-dimensional cell if exactly m values in  $\{a_1, a_2, ..., a_n\}$  are not \*
- Base cell: m=n
- Aggregate cell: m<n</p>

#### **Cell Examples**

◆C1: (\*,\*,\*,LA,80K)
◆C2: (M,\*,\*,LA,100K)
◆C3: (M,20-30,HS,LA,100K)
◆C4: (F,\*,\*,SD,35K)
◆C5: (\*,\*,\*,SD,33K)

## Ancestor and Descendent Cells

- An i-D cell a=(a<sub>1</sub>, a<sub>2</sub>, ..., a<sub>n</sub>, measure<sub>a</sub>) is
   an ancestor of a j-D cell
   b=(b<sub>1</sub>, b<sub>2</sub>, ..., b<sub>n</sub>, measure<sub>b</sub>) iff
   i <j, and</pre>
- For  $1 \le m \le n$ ,  $a_m = b_m$  whenever  $a_m \ne *$
- a is a parent of b (and b a child of a)
  - $\hfill\blacksquare$  a is an ancestor of b, and
  - ∎ j=i+1

### Ancestor and Descendent Examples

◆C1: (\*,\*,\*,LA,80K)
◆C2: (M,\*,\*,LA,100K)
◆C3: (M,20-30,HS,LA,100K)
◆C4: (F,\*,\*,SD,35K)
◆C5: (\*,\*,\*,SD,33K)

#### **Closed Cell**

A cell c is a closed cell if there is no descendent of c that has the same measure as c

#### **Closed Cell Examples**

- Which of the following are *closed* cells??
  - C1: (\*,\*,\*,LA,80K)
  - C2: (M,\*,\*,LA,100K)
  - C3: (M,20-30,HS,LA,100K)
  - C4: (F,\*,\*,SD,35K)
  - C5: (\*,\*,\*,SD,33K)

Close	Closed Cube					
◆A coof	A closed cube is a data cube consisting of only closed cells What's the closed cube of the following data??					
rid	gender	age	education	address	salary	
1001	М	24	High school	LA,CA	100K	
1002	F	25	College	LA,CA	60K	





Order Matters				
rid	gender	age	education	salary
1001	м	20-30	High school	100K
1003	м	30-40	College	65K
1008	м	40-50	< High School	30K
1004	м	>60	Graduate school	120K
1005	F	<20	College	40K
1002	F	20-30	College	60K
1006	F	20-30	Graduate school	50K
1007	F	50-60	High school	35K













#### About BUC

- ♦It is actually *Top-Down*
- Dimensions should be processed in order of decreasing cardinality
- Take advantage of the Apriori property
- Does not share computation costs between parent and child group-bys (unlike Star-Cubing)

# Dealing with Non-Monotonic Measures

## Transform Non-monotonic Measures

- Cell c covers n non-empty base cells
- $avg^k(c)$  : the average of top k base cells covered by c
- ♦count≥k and  $avg≥x \rightarrow avg^k(c)≥x$ 
  - What if we remove the count≥k condition??

### Problems of Iceberg Cubes

- May still be too large
- Incremental updates require recomputation of the whole cube
- Minimum support is hard to determine

#### **Cube Shells**

- Observation: most OLAP operations are performed on a small number of dimensions at a time
- A cube shell of a data cube consists of the cuboids up to a certain dimension
  - E.g. all cuboids with 3 dimensions or less in a 60-dimension data cube

#### Problems with Cube Shells

- They may still be too large
  - E.g. how many cuboids in a 3-D shell of a 60-D data cube??
- They can't be used to answer queries like

(location,product\_type,suppli
er,2004,?)

#### Shell Fragments

- Compute only parts of a cube shell shell fragments
- Answer queries using the precomputed data

#### Shell Fragment Example tid а b с d е 1 $\mathsf{a}_1$ $b_1$ $C_1$ $\mathsf{d}_1$ $e_1$ 2 a<sub>1</sub> b<sub>2</sub> c<sub>1</sub> d<sub>2</sub> $e_1$ 3 $a_1$ $b_2$ $c_1$ $d_1$ $e_2$ 4 $\mathsf{a}_2 \quad \mathsf{b}_1 \quad \mathsf{c}_1 \quad \mathsf{d}_1 \quad \mathsf{e}_2$ 5 a<sub>2</sub> b<sub>1</sub> $c_1 \quad d_1$ e3

# Shell Fragments Computation (1)

Partition the dimension into nonoverlapping groups – fragments

 $(a,b,c,d,e) \rightarrow (a,b,c)$  and (d,e)

# Shell Fragments Computation (2)

Scan the base cuboid and construct an inverted index for each attribute

Attribute value	TID list	List size
a <sub>1</sub>	{1,2,3}	3
a <sub>2</sub>	{4,5}	2
	<i>( , , =</i> )	

D <sub>1</sub>	{1,4,5}	3	
b <sub>2</sub>	{2,3}	2	
C1	{1,2,3,4,5}	5	
d <sub>1</sub>	{1,3,4,5}	4	
d <sub>2</sub>	{2}	1	
e <sub>1</sub>	{1,2}	2	
e <sub>2</sub>	{3,4}	2	
e <sub>3</sub>	{5}	1	

# Shell Fragments Computation (3) ...

- Compute the full *local* data cube (except the local apex cuboid) for each fragment
  - Vs. Cube shell??
- Record an inverted index for each cell in the cuboids

 $(a,b,c) \rightarrow a, b, c, ab, ac, bc, abc (d,e) \rightarrow d, e, de$ 

#### ... Shell Fragment Computation (3) ...

#### ab cuboid

Cell	Intersection	TID List	List Size
(a <sub>1</sub> ,b <sub>1</sub> )	$\{1,2,3\} \cap \{1,4,5\}$	{1}	1
(a <sub>1</sub> ,b <sub>2</sub> )	{1,2,3} ∩ {2,3}	{2,3}	2
(a <sub>2</sub> ,b <sub>1</sub> )	{4,5} ∩ {1,4,5}	{4,5}	2
(a <sub>2</sub> ,b <sub>2</sub> )	{4,5} ∩ {2,3}	0	0

- Inverted indexes are built as the cell aggregates are computed
- Apriori property can be used to prune some computation

Shell Fragment Computation (3)			Query Cube Fragments – Point Query		
Using an ID the original          TID         1         2         3         4         5	D_measure database item_count 5 3 8 5 2	array instead of table	<ul> <li>Point query: all dimensions are instantiated with either a value or *</li> <li>Examples: <ul> <li>(a<sub>1</sub>,b<sub>2</sub>,c<sub>1</sub>,d<sub>2</sub>,e<sub>1</sub>,??)</li> <li>(a<sub>1</sub>,b<sub>2</sub>,c<sub>1</sub>,d<sub>2</sub>,*,??)</li> <li>(*,b<sub>2</sub>,c<sub>1</sub>,d<sub>2</sub>,*,??)</li> </ul> </li> </ul>		





## Further Issues in OLAP

Detect exceptions

- Data visualization and exploration
- Complex aggregations
  - E.g. total sales of highest-priced items group by month and region
- ♦Gradient analysis
  - Changes between probe cells and its ancestors, descendents, and siblings